

Performance of Parallel Operated Hydro Turbine driven DFIGs in Three Phase Four Wire System

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Abstract— We report our first-principles studies on the linear and non-linear optical properties of ferroelectric polyvinylidene fluoride crystal. Calculated values of the refractive indices agree well with experiments. As regards the second-harmonic-generation coefficients, theoretical values are larger than experimental ones. Possible reasons for the discrepancy are discussed.

INTRODUCTION

Polyvinylidene fluoride (PVDF) and its copolymers with trifluoroethylene (TrFE) have been studied extensively due to their unique piezoelectric, pyroelectric, and ferroelectric properties. They are widely used in industry as low-cost electromechanical devices such as transducers and detectors. Furthermore, the ferroelectric phases of PVDF copolymer crystals also have good non-linear optical (NLO) properties. They have quite large optical windows (1200–200 nm), which makes them good candidates for use as frequency conversion materials working in the ultraviolet region. They can also be used in optical memory devices. In addition, the NLO quality of this material can be significantly improved by hosting molecules of high NLO susceptibility in the amorphous region, which is a great advantage of polymers.

Literature Survey

Experimentally, there are many reports on the determination of the optical constants of PVDF. However, the crystalline polymers used in experiments often consist of crystalline regions comprising micro crystals and non-crystalline areas between the micro crystals and the orientations of micro crystals in the samples used in experiments generally have a broad distribution. Thus those experimental values differ substantially from each other. As regards the theoretical side, to our knowledge, there has been only very limited investigation of the optical properties of this material. Cakmak and Wang and Spector and Stein

have given reports on the refractive indices of PVDF. However, their quantum chemistry calculations strongly depend on the choices of bond parameters, which results in a large uncertainty. Thus it is necessary to carry out a first-principles study on the optical properties of single-crystal PVDF, which is a starting point for understanding the microscopic mechanism governing the optical behaviours of the complicated specimens used in experiments.

In a recent letter, we reported theoretical results on the energy band structure and band symmetries of PVDF. The calculated results agree well with photoemission experiments. As a further step, in this paper, we report our first-principles calculation of the linear and NLO constants of the ferroelectric phase (the polar β -phase, form I) of PVDF.

Band Structure

The first-principles band structure approach applied in this work is the full-potential linear-augmented-plane-wave (FLAPW) method. The exchange–correlation potential is treated in the generalized gradient approximation (GGA) of density functional theory.

The crystal structure and calculation details such as the cut-off energy, muffin-tin radii, and band structure, are presented in our previous work. Here it is important to point out that the b-axis in our calculation is the polar axis, whereas the c-axis is the chain axis of PVDF. The energy band structure and density of states (DOS) of PVDF are presented in figure 1 for the convenience of later discussion.

In this work, we adopt the formalism of Hughes and Sipe to calculate the optical susceptibilities. Their formula used in the calculation of SHG coefficients was rearranged by Rashkeev to show Kleinman symmetry explicitly. Lin improved the formula in the static limit by avoiding possible divergent terms; thus they were able to achieve

good convergence on the k-point sampling, as we did before by using a different formula that does not present Kleinman symmetry explicitly. Here we point out that the formula of Lin et al can be further simplified by abandoning the so-called two-band term, which can be proved to be zero after some straightforward algebra. Specifically, the expression for $\chi^{(2)}$ in the static limit can be written as

$$\chi_{ijk}^{(2)} = -\frac{e^3}{2\hbar^2 m^3} \int_{BZ} \frac{dk}{4\pi^3} P(ijk) \left[\sum_{v'c} \text{Im}(p_{v'v}^i p_{v'c}^j p_{c'c}^k) \left(\frac{1}{\omega_{c'v'}^3 \omega_{c'v}^2} + \frac{2}{\omega_{c'v}^4 \omega_{c'v'}} \right) \right] \quad (1)$$

$$+ \sum_{vc} \text{Im}(p_{cv}^i p_{vc}^j p_{c'c}^k) \left(\frac{1}{\omega_{c'v}^3 \omega_{c'v}^2} + \frac{2}{\omega_{c'v}^4 \omega_{c'v'}} \right)$$

where i, j, k are Cartesian components, P(ijk) denotes full permutation over i, j, k and explicitly shows Kleinman symmetry of the SHG coefficients, v (v') and c (c') denote valence and conduction bands, respectively. p_{mn} is the momentum matrix element connecting states m and n and the band energy difference is denoted as $\hbar\omega_{mn}$. Scissors operators are introduced to overcome the band gap underestimation problem. In this calculation, the energy shift is chosen to be 0.6 eV to fit the experimental band gap. Since the calculated energy gap is very close to the experimental one in our case, there is no need to use other sophisticated techniques applied in theoretical studies of the optical properties of polymer materials such as polyacetylene. Furthermore, the validity of the scissors approximation is strongly supported by recent SHG experiments on GaAs.

The linear optical properties of PVDF are investigated using 48 special k-points in the irreducible Brillouin zone. The results are very good on k-points convergence. The difference between the dielectric constants obtained with 12 and 48 k-points is within 0.5%. Since the system that we studied is a perfect biaxial crystal with orthorhombic structure, there are three different principal indices of refraction, i.e., n_a , n_b and n_c , in which a, b, and c represent the photon polarization directions along the crystal axes a, b, and c, respectively.

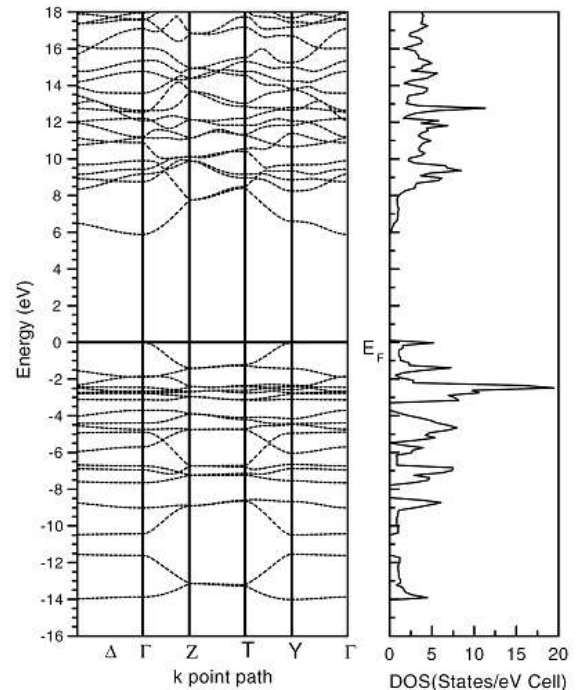


Figure 1. The calculated band structure and DOS of PVDF.

Calculated values of the refractive indices are listed in Table 1, together with corresponding experimental and other theoretical values. In fact the formula used to calculate the refractive indices is well documented and ours is taken from. As we can see from the table, the magnitudes of our calculated refractive indices agree well with observations. However, the agreement of the anisotropic orders is not good. Our calculations found $n_a > n_c > n_b$, whereas experimental results show that n_c has the largest value. The dispersions of the refractive indices are plotted in figure 2. Assuming that the wavelength of the incident light is 1.06 μm , we obtained the average dispersion as $n_{2\omega} - n_{\omega} = 0.0082$, very close to the experimental value 0.0077. We also noticed that n_c becomes larger than n_a after 4.5 eV.

Figure 3 shows the calculated linear absorption spectra for the three different polarization directions of PVDF. As can be seen from the figure, the anisotropic structure is quite obvious, i.e., the absorption of the direction c (the chain direction) starts from about 6.5 eV, corresponding to the value of the energy gap, whereas the absorptions of the other two directions (perpendicular to the chain) start from almost 8 eV. As we can see from figure 1, the short terrace that starts at 6.5 eV and extends about 2 eV at the lower end of the conduction bands in the DOS plot is solely formed by the first conduction band, which mainly consists of C 2p electron states. A detailed oscillator strength analysis reveals that the first peak in the plot of the absorption coefficients corresponds to the transition from the highest

occupied molecular orbital in which F 2p states are dominant to the lowest unoccupied molecular orbital. And only the transition along the chain direction is favourable. This again reveals the one-dimensional nature of the PVDF crystal.

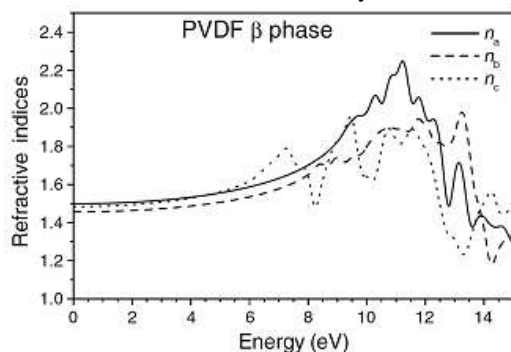


Figure 2. Calculated dispersion curves for the refractive indices of PVDF. Labels a, b, and c represent the photon polarization directions along the crystal axes a, b, and c, respectively.

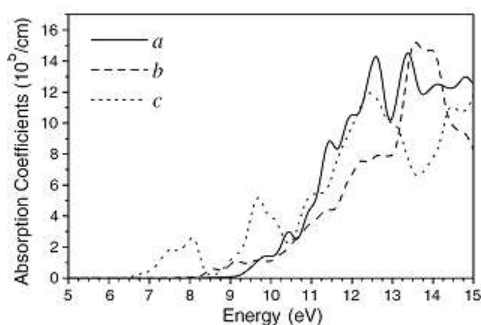


Figure 3. Linear absorption coefficients of PVDF.

Table 1. Refractive indices of PVD crystal.

	n_a	n_b	n_c
Theory			
Current	1.499	1.456	1.484
Cakmak and Wang ^a	1.545	1.522	1.448
	1.483	1.548	1.629
Experiment			
Broussoux and Micheron ^b	1.436	1.425	1.444

^aReference [12].

^bReference [7].

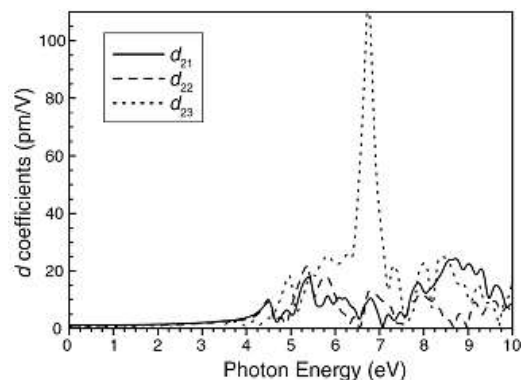


Figure 4. Calculated dispersion curves for the d-coefficients of PVDF.

Table 2. SHG coefficients d_{21} , d_{22} , d_{23} for PVDF crystal, in units of pm V^{-1}

	d_{21}	d_{22}	d_{23}
Theory	2.01	1.66	0.26
Experiment ($\lambda=1060 \text{ nm}$)			
Bergman <i>et al</i> ^a	0.23	0.47	-0
Berge <i>et al</i> ^b	0.05	0.22	0.05

^aReference [2].

^bReference [8].

Then we calculated the SHG coefficients of the β -phase of PVDF. Since the point group of PVDF is C_{2v} ($mm2$) and the b-axis is the twofold symmetry axis, there are three independent SHG components, i.e.,

$$\left(= \frac{1}{2} \chi_{211}^{(2)}, d_{22} (= \frac{1}{2} \chi_{222}^{(2)}) \text{ and } d_{23} (= \frac{1}{2} \chi_{233}^{(2)}) \right).$$

The calculated results and available experimental values are listed in table 2 for comparison. As we can see from the table, the theoretical values are much larger than the experimental values. From the dispersion curves of the d-coefficients (see figure 4), we can see that the behaviours of the components d_{21} and d_{22} are quite similar. The component d_{23} is rather small in the static limit, but it becomes quite large after 3.5 eV and reaches its extremely large peak value at around 7 eV. However, SHG experiments in that energy range are rarely carried out, so data were scarce.

PVDF has important applications because of its electro-optical properties. Using the relationship between the linear electro-optical (LEO) coefficients r_{abc} and the SHG coefficients χ_{abc} in the static limit, i.e.,

$$r_{abc} = -\frac{2\chi_{abc}}{n_a^4}, \quad (2)$$

where a, b, c are Cartesian components and n_a is the index of refraction in the a-direction, we found the three independent LEO coefficients r_{211} , r_{222} , and r_{233} to be 1.78, 1.48, and 0.23 pm V^{-1} , respectively. Again, these values are much larger than the experimental values 0.21, 0.38, and 0.10 pm V^{-1} .

We attribute these discrepancies, together with the mismatch of the theoretical and experimental anisotropic orders of the refractive indices, to the fact that the samples used in those experiments are not perfect single crystals, or not even single phase. For example, the chain axes of the specimens used by Berge are randomly oriented in the plane of the film. Thus their SHG coefficients d_{21} and d_{23} are equal. In such cases, the refractive indices and SHG coefficients are actually averaged values. The orientation problem may not be very serious in the linear case, but in the determination

of non-linear coefficients that are strongly orientation dependent; this would make a big difference.

Another important factor which causes a discrepancy between the theory and experiments is the copolymer effect. As is well known, the samples most widely used experimentally are actually PVDF copolymers (P (VDF-TrFE), 70:30). To study the copolymer effect, we calculated the optical constants of PTrFE, whose electronic structure has also been studied in our previous work. We found that the average values of the refractive indices changed significantly from PVDF (1.48) to PTrFE (1.29). And the anisotropic order of PTrFE ($n_c > n_a > n_b$) is also different from that of PVDF. Thus we were able to confirm that the replacement of hydrogen atoms with fluorine atoms will reduce the overall refractive index of the polymer, which agrees with the conclusion of Cakmak and Wang. In the non-linear case, the copolymer effect is even more obvious, since PTrFE has a different point group to PVDF and thus different independent SHG components.

[4] Kepler R G and Anderson R A 1978 J. Appl. Phys. 49 1232

Conclusion

In summary, we have studied the linear and NLO properties of PVDF by means of a first-principles calculation. The values of the calculated refractive indices are in good agreement with experiments. But the anisotropic order of the refractive indices is different from the observations. We also calculated the SHG and LEO coefficients of this material. The agreement with experiments is not good. We attribute these discrepancies to the non-single crystal samples used in experiments and the copolymer effect. However, other factors such as temperature and surface and local field corrections may also play important roles. Our calculations, unlike previous quantum chemistry analysis, give an unambiguous prediction of the optical properties of the ideal β -phase of PVDF, which might be helpful for determining the actual orientation of the molecular axis in films used in experiments.

References

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